

## Atlantean Dodgeball

## Guide and Answer Key for Instructors

The Atlantean Dodgeball animation is available on iTunes $U$ (search "Math Snacks") and at mathsnacks.org

## Learning Objectives: The Atlantean

Dodgeball animation is about ratios and differences. By watching the animation, completing the activities in the Learner Guide, and completing at least one bonus activity, students will:

- Understand that ratios can represent part:part or part:whole relationships.
- Demonstrate how part:whole ratios can be represented as fractions, converted to decimals, and converted to percentages.
- Be able to find equivalent ratios using various methods.


## Animation Discussion

With your students, watch the 6-minute animation Atlantean Dodgeball at http://www.mathsnacks.org and spend about 10 minutes discussing the big ideas or key points in the animation.

- Compare and contrast how the two coaches compared their team sizes throughout the game. (Draw out the difference between part:part ratios and the absolute numerical sizes of the teams.)
- Why was it more useful when the coaches considered the ratio of players on the teams rather than the difference in the number of players on the teams?
- Did the graphs in the animation help you understand how each team was doing in the tournament?

Vocabulary ratio, part:part, part:whole, fraction, equivalent ratio, equivalent fraction, decimal, percentage


## Learner Guide Page 2




## Bonus Activities

Select one or more of these activities to do with your students after they have completed the Learner Guide.

1. Divide students into small groups. Each group should try to convince the Belugas' coach to worry about the team-to-team ratio of players rather than the absolute difference in the number of players. They may create a skit, draw charts or pictures, or use props (e.g., books, chairs) to illustrate their points. A spokesperson for each group should present its case. (Estimated time: 20 min . to one class period).
2. Organize a dodgeball game with students in the class using appropriate balls (ask a PE teacher). Keep track of the ratios after each round or after each game. Have students create a chart with the various ratios and have them discuss the similarities and differences between the ratios-emphasize the relationship between the ratios in the game and a 1:1 ratio.
3. Ask the teams to calculate the player-player ratios and simplify them for the data presented in the table below. Calculators may be allowed. The instructor should call out the stats. For example, say, "Astros 48, Stars 8." The first team to give the reduced ratio 6:1 gets a point. Blank tables are provided on page 6 if needed as handouts.

| Team 1 | Players | Team 2 | Players | Ratio |
| :---: | :---: | :---: | :---: | :---: |
| Astro | 48 | Stars | 8 | $6: 1$ |
| Pelicans | 24 | Dolphins | 12 | $2: 1$ |
| Dawgs | 65 | Kook Kats | 15 | $13: 3$ |
| Tigers | 14 | Lions | 63 | $2: 9$ |
| Reds | 1 | Blues | 73 | $1: 73$ |
| Bears | 143 | Cubs | 39 | $11: 3$ |
| Panthers | 100 | Lions | 10 | $10: 1$ |
| Spiders | 60 | Scorpions | 30 | $2: 1$ |
| Knights | 45 | Lances | 60 | $3: 4$ |
| Mustangs | 12 | Colts | 52 | $3: 13$ |
| Pirates | 99 | Steelers | 18 | $11: 2$ |
| Jays | 21 | Cardinals | 63 | $1: 3$ |
| Cowboys | 56 | Wranglers | 11 | $56: 11$ |
| Hawks | 102 | Eagles | 22 | $51: 11$ |

## Bonus Activities

4. Last baseball season, the teams listed in the table below each played 144 games. Ask students to figure each team's win-loss ratio. This activity may be done by teams or by individuals; or assign a few teams to each person in the class. (For example, if you have 7 students, ask each student to figure the ratios for 4 teams.) Which teams had winning seasons? Blank tables are provided on page 6 if needed as handouts.
If it is appropriate mathematically for some or all of the students in your class, have students calculate the win:total ratio and the loss:total ratio as well. However, be prepared to lead an appropriate discussion about the differences between these types of ratios.
Answers: Bears (143:1) Panthers (25:11) Pirates (11:5) Blues (73:71)

| Teams | Wins | Losses | Wins/Losses | Teams | Wins | Losses | Wins/Losses |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Astro | 48 | 96 | $48: 96$ or $1: 2$ | Stars | 8 | 136 | $8: 136$ or $1: 17$ |
| Pelicans | 24 | 120 | $24: 120$ or $1: 5$ | Dolphins | 12 | 132 | $12: 132$ or $1: 11$ |
| Dawgs | 65 | 79 | $65: 79$ | Kook Kats | 15 | 129 | $15: 129$ or $5: 43$ |
| Tigers | 14 | 130 | $14: 130$ or $7: 65$ | Lions | 63 | 81 | $63: 81$ or $7: 9$ |
| Reds | 1 | 143 | $1: 143$ | Blues | 73 | 71 | $73: 71$ |
| Bears | 143 | 1 | $143: 1$ | Cubs | 39 | 105 | $39: 105$ or $13: 35$ |
| Panthers | 100 | 44 | $100: 44$ or $25: 11$ | Lions | 10 | 134 | $10: 134$ or $5: 67$ |
| Spiders | 60 | 84 | $60: 84$ or $5: 7$ | Scorpions | 30 | 114 | $30: 114$ or $5: 19$ |
| Knights | 45 | 99 | $45: 99$ or $5: 11$ | Lances | 60 | 84 | $60: 84$ or $5: 7$ |
| Mustangs | 12 | 132 | $12: 132$ or $1: 11$ | Colts | 52 | 92 | $52: 92$ or $13: 23$ |
| Pirates | 99 | 45 | $99: 45$ or $11: 5$ | Steelers | 18 | 126 | $18: 126$ or $1: 7$ |
| Jays | 21 | 123 | $21: 123$ or $7: 41$ | Cardinals | 63 | 81 | $63: 81$ or $7: 9$ |
| Cowboys | 56 | 88 | $56: 88$ or $7: 11$ | Wranglers | 11 | 56 | $11: 56$ |
| Hawks | 102 | 42 | $102: 42$ or $51: 21$ | Eagles | 22 | 11 | $22: 11$ or $2: 1$ |

## Page 1 Answer Key

1. In the Atlantean dodgeball tournament, both teams had lost about half of their members going into the final round. The Sea Urchins' coach looked at the team sizes of 500 and 480 and was happy that the teams were still fairly evenly matched (close to a $1: 1$ ratio). The Belugas' coach was upset because the Sea Urchins had 20 more players (a 20-player difference).
a. Fill in the empty bar graphs to estimate the ratios of Sea Urchins to Belugas as the score changes during the tournament.

b. A newspaper reports that the final ratio of the tournament was 2:9. Are they correct? Why or why not?
Answer: If the paper reported the ratio of Belugas to Sea Urchins as 2:9, it would be correct, but if it did not specify Belugas to Sea Urchins it could be interpreted wrongly.

## Page 1 continued Answer Key

2. Here are three pie charts that show wins and losses as parts of the total games played. Fill in the empty circle with the ratio of wins to losses for Metro City.

| Small Town lost $\mathbf{2 0}$ out <br> of $\mathbf{5 0}$ games | Big City lost $\mathbf{1 6}$ out of <br> $\mathbf{6 4}$ games | Metro City lost $\mathbf{9}$ out of <br> $\mathbf{4 5}$ games |  |
| :--- | :--- | :--- | :--- |
|  |  |  |  |

a. Who do you think is the biggest loser? Why?

Answer: Small town. Justifications may vary. One answer would be that Small Town lost 40\%, Big City lost 25\%, Metro City lost 20\%.
b. What is the ratio of games lost to total games for each team? Write your answer as a fraction.

| Team Name | Ratio | Fraction | Simplified Fraction | Decimal | Percentage of games lost |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Small Town | $20: 50$ | $20 / 50$ | $2 / 5$ | 0.40 | $40 \%$ |
| Big City | $\mathbf{1 6 : 6 4}$ | $\mathbf{1 6 / 6 4}$ | $\mathbf{1 / 4}$ | $\mathbf{0 . 2 5}$ | $\mathbf{2 5 \%}$ |
| Metro City | $\mathbf{9 : 4 5}$ | $\mathbf{9 / 4 5}$ | $\mathbf{1 / 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{2 0 \%}$ |

## Page 2 Answer Key

3. You and your friend, Joe, are arguing about which baseball team is the best. Big City's baseball team, Joe's favorite, had 48 wins and 16 losses for the season. You think your team, Metro City, has a better record because it lost fewer games. Joe thinks his team has a better record because they won more games. Try to settle the argument by filling out the table below.

| Team | Games | Wins | Losses | Win to Loss Ratio | Wins to Total Ratio | Losses to Total Ratio |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Small Town | $\mathbf{5 0}$ | $\mathbf{3 0}$ | $\mathbf{2 0}$ | $30: 20$ | $30: 50$ | $20: 50$ |
| Big City | 64 | $\mathbf{4 8}$ | 16 | $48: 16$ | $48: 64$ | $16: 64$ |
| Metro City | 45 | 36 | 9 | $36: 9$ | $36: 45$ | $9: 45$ |

a. How are the ratios of Win:Loss, Wins:Total, and Losses:Total related?

Answer: Total = Wins + Losses
b. Use one or all of these ratios to decide which team has the best record for the season. Explain your answer and show your work.

Answers will vary, but reasoning should be similar to that in $2 c$ or 3 a of Bonus Activities.
4. 9:1 is the ratio of Sea Urchin players to Beluga players. Is this a part-to-part or part-to-whole ratio?

Answer: Part-to-part
a. Describe how this ratio can be represented in fraction form.

Answer: Fractions represent part-to-whole relationships, so the fraction representation of the 9:1 ratio can be written as follows: 1/10 of the players left are Belugas and 9/10 of the players left are Sea Urchins. Emphasize the importance of labeling.

| Common Core State Standards of Mathematics |  |
| :--- | :--- |
| 6.RP | Understand ratio concepts and use ratio reasoning to solve problems. |
| 6.RP. 1 | Understand the concept of a ratio and use ratio language to describe a ratio relationship <br> between two quantities. |
| 6.RP.2 | Understand the concept of a unit rate a/b associated with the ratio a:b with b not equal to 0, <br> and use rate language in the context of a ratio relationship. |
| 6.RP.3 | Use ratio and rate reasoning to solve real-world and mathematical problems, e.g. by <br> reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or <br> equations. |
| 7.RP | Ratios and Proportional Relationships |
| 7.RP.1 | Compute unit rates associated with ratios and fractions, including ratios of lengths, areas and <br> other quantities measured in like or different units. |
| 7.RP.2 | Recognize and represent proportional relationships between quantities. |
| 7.RP.3 | Use proportional relationships to solve multistep ratio and percent problems. |

Math Snacks animations, games and support materials address all of the Common Core State Standards for Mathematical Practices when used as recommended in the teacher guide.

| Player-player ratios |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Team 1 | Players | Team 2 | Players | Answer |
| Astro | 48 | Stars | 8 |  |
| Pelicans | 24 | Dolphins | 12 |  |
| Dawgs | 65 | Kook Kats | 15 |  |
| Tigers | 14 | Lions | 63 |  |
| Reds | 1 | Blues | 73 |  |
| Bears | 143 | Cubs | 39 |  |
| Panthers | 100 | Lions | 10 |  |
| Spiders | 60 | Scorpions | 30 |  |
| Knights | 45 | Lances | 60 |  |
| Mustangs | 12 | Colts | 52 |  |
| Pirates | 99 | Steelers | 18 |  |
| Jays | 21 | Cardinals | 63 |  |
| Cowboys | 56 | Wranglers | 11 |  |
| Hawks | 102 | Eagles | 22 |  |


| Win-loss ratio |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Teams | Wins | Answer | Teams | Wins | Answer |
| Astro | 48 |  | Stars | 8 |  |
| Pelicans | 24 |  | Dolphins | 12 |  |
| Dawgs | 65 |  | Kook Kats | 15 |  |
| Tigers | 14 |  | Lions | 63 |  |
| Reds | 1 |  | Cubs | 39 |  |
| Bears | 143 |  | Scorpions | 30 |  |
| Panthers | 100 |  | Lances | 60 |  |
| Spiders | 60 |  | Colts | 52 |  |
| Knights | 45 |  | Steelers | 18 |  |
| Mustangs | 12 |  | Cardinals | 63 |  |
| Pirates | 99 |  | Wranglers | 11 |  |
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