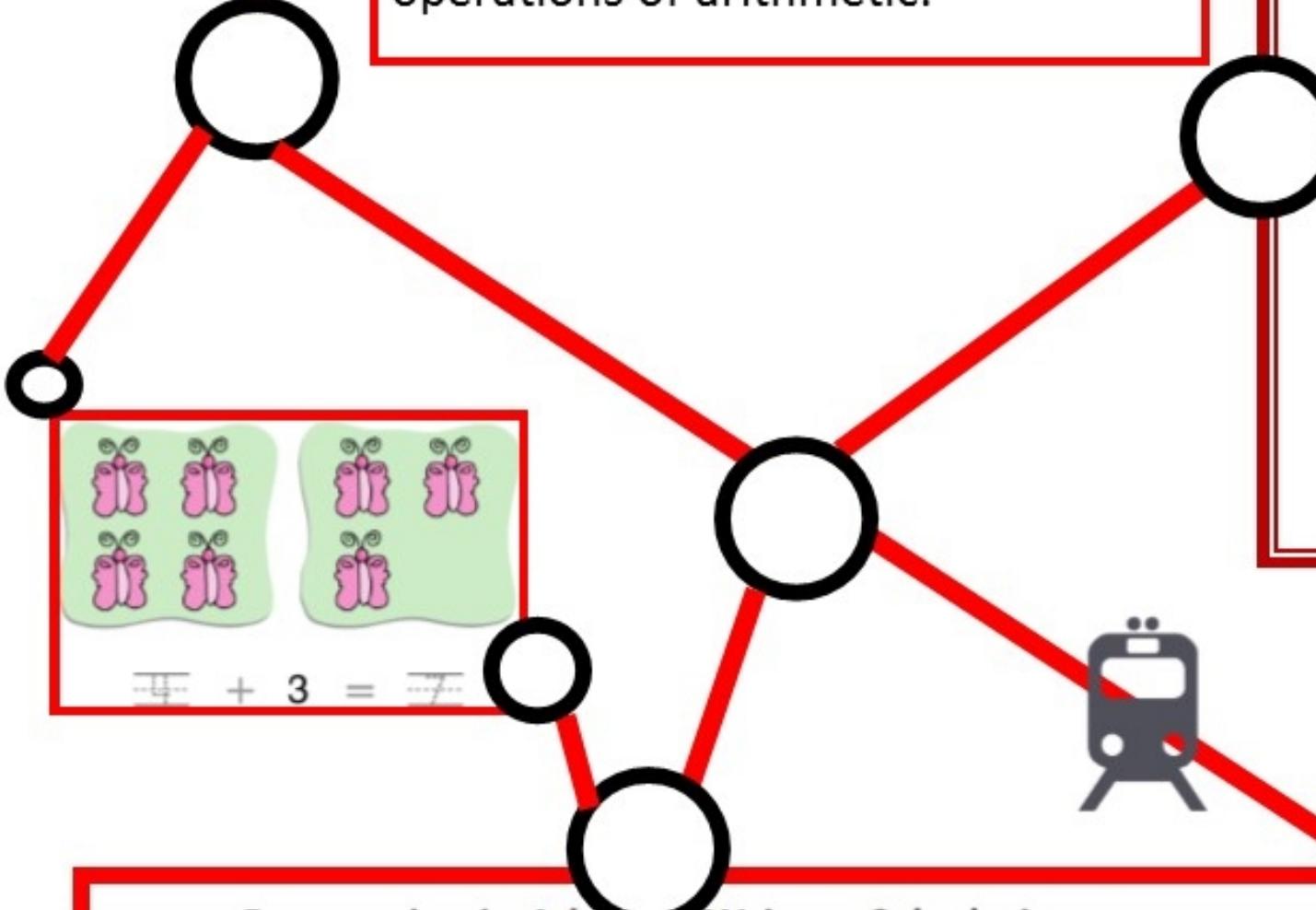




UNDERGROUND

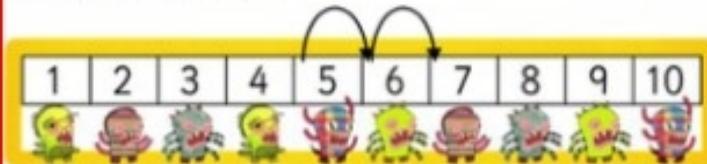
**Addition** (often signified by the plus symbol "+") is one of the four basic operations of arithmetic.



### Progression in Addition Written Calculations

#### EYFS

Number Tracks:  $4 + 2 = 6$



Prepared Number Line:  $4 + 3 = 7$



#### Key Stage 1 (Yr 1/2)

Prepared Number Line:  $4 + 3 = 7$



Prepared Number Line:

$$16 + 12 = 28$$

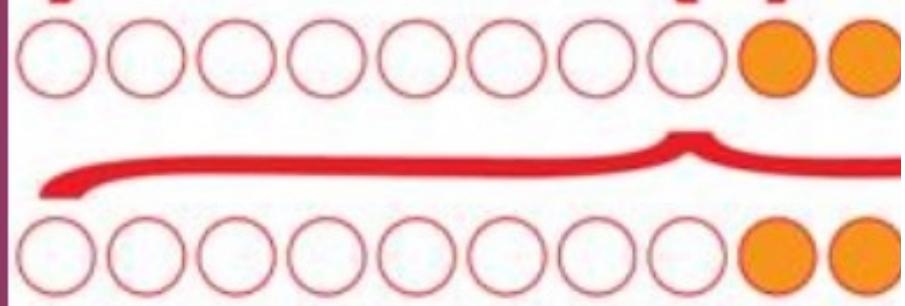


Unnumbered Number Line:  $23 + 13 = 36$

## Vocabulary

+  
Add  
Addition  
Plus  
And  
Count on  
More  
Sum  
Total  
Altogether  
Increase

$$8 + 7 = 15$$



Inverse



**Subtraction**  
that represents objects from the minus sign.

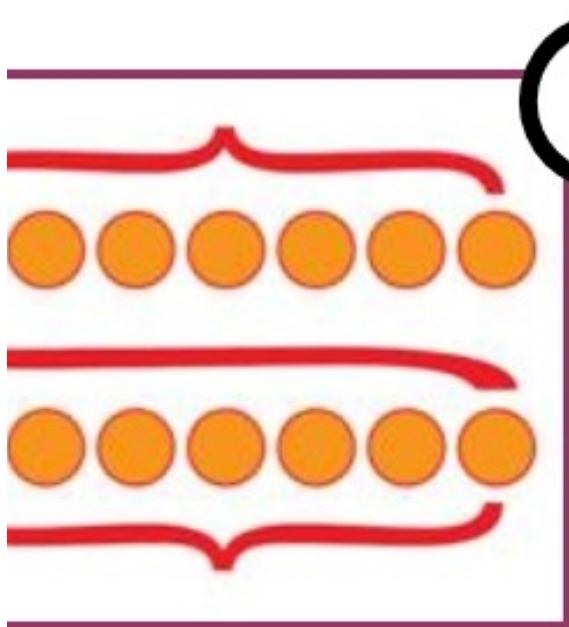
1/2)

Hundred Square:

$$34 + 13 =$$

$$34 + 10 + 3 = 47$$

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80



### Vocabulary

Subtract

Take Away

Minus

Less

Fewer

Difference

**Subtraction** is a mathematical operation that represents the operation of removing objects from a collection. It is signified by the minus sign (-)



## Progression in Subtraction Written Calculations

### EYFS

Number Tracks:  $10 - 5 = 5$



Prepared Number Line:  $9 - 5 = 4$



### Lower Key Stage 2 (Yr 3/4)

Expanded column method, starting with least significant digits (in preparation for formal method), paying attention to place value of each digit. By the end of Year 3, pupils should move onto the formal method with three digits and by the end of Year 4, the formal method with four digits.

$567 - 276$ :

$$\begin{array}{r}
 \text{H} \quad \text{T} \quad \text{U} \\
 400 \ 160 \\
 \cancel{500} \ \cancel{60} \ 7 \\
 - 200 \ 70 \ 6 \\
 \hline
 200 \ 90 \ 1 \quad = 291
 \end{array}$$

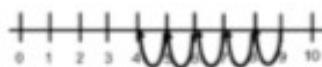
$$\begin{array}{r}
 \text{Th} \quad \text{H} \quad \text{T} \quad \text{U} \\
 4 \cancel{7} \ 13 \ 6 \cancel{1} 0 \\
 - \quad 4 \ 5 \ 5 \ 3 \\
 \hline
 0 \ 8 \ 1 \ 7
 \end{array}$$

For column methods of subtraction, the subtraction sign will be positioned on the left.

Where exchanging takes place, this will be recorded above the starting number.

### Key Stage 1 (Yr 1/2)

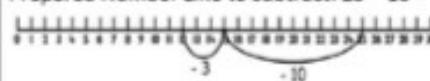
Prepared Line to take away:  $9 - 5 = 4$



On a hundred square:

11 - 24 = 13 (Find the position number)									
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Prepared Number Line to subtract:  $25 - 13 = 12$



Prepared number line to find the difference (counting on):

$25 - 13 = 12$



### Upper Key Stage 2 (Yr 5/6)

Subtracting whole numbers with more than four digits as well as decimal numbers to the thousandths:

$$\begin{array}{r}
 5 \ 12 \ 9 \\
 7 \cancel{6} \cancel{1} 15 \\
 - 4 \ 5 \ 5 \ 3 \ 7 \\
 \hline
 3 \ 0 \ 7 \ \cancel{6} \ 8
 \end{array}$$

For column methods of subtraction, the subtraction sign will be positioned on the left.

$$\begin{array}{r}
 7 \ 15 \ 9 \ 9 \ 14 \\
 \cancel{6} \cancel{7} \cancel{8} \cancel{9} . \cancel{1} 4 \ 7 \\
 - 2 \ 7 \ 6 \ 2 \ . \ 8 \ 5 \ 3 \\
 \hline
 5 \ 8 \ 3 \ 7 \ . \ 6 \ 9 \ 4
 \end{array}$$

Where exchanging takes place, this will be recorded above the starting number.



$$\underline{\underline{7}} \quad - \quad 4 \quad = \quad \underline{\underline{3}}$$

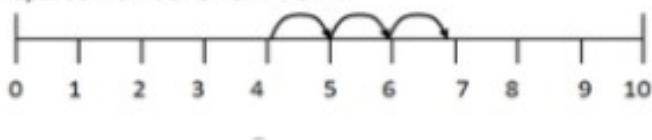
## Vocabulary

X

Lots of  
Groups of  
Times  
Multiply



Prepared Number Line:  $4 + 3 = 7$



Unnumbered Number Line:  $23 + 13 = 36$



### Lower Key Stage 2 (Y3/4)

Expanded column method, starting with least significant digits (in preparation for formal method), paying attention to place value of each digit.

Moving on to formal method, carrying numbers below the line.

$$\begin{array}{r} \text{H T U} \\ 1 3 5 \\ + 4 4 \\ \hline 9 \\ 7 0 \\ 1 0 0 \\ \hline 1 7 9 \end{array}$$

$$\begin{array}{r} \text{Th H T U} \\ 3 5 9 6 \\ + 1 8 7 4 \\ \hline 1 0 \\ 1 6 0 \\ 1 3 0 0 \\ \hline 4 0 0 0 \\ \hline 5 4 7 0 \end{array}$$

$$\begin{array}{r} \text{Th H T U} \\ 3 5 9 6 \\ + 1 8 7 4 \\ \hline 1 1 1 \\ 5 4 7 0 \end{array}$$

$$\begin{array}{r} 4 2 6 9 4 \\ + 5 5 5 0 6 \\ \hline 9 8 2 0 0 \\ 1 1 1 \end{array}$$

$$\begin{array}{r} 5 1 2 7 . 3 4 6 \\ + 2 7 6 2 . 8 2 3 \\ \hline 7 8 9 0 . 1 6 9 \\ 1 1 \end{array}$$

### Upper Key Stage 2 (Yr 5)

Adding whole numbers with more than four digits; numbers to the thousandths:

### Progression in Division Written Calculations

#### EYFS

Not appropriate for the year group.

#### Key Stage 1 (Yr 1/2)

Written numberline used for repeated subtraction:

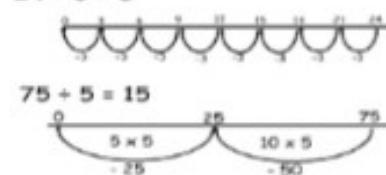
$$15 \div 5 = 3$$



Blank numberline used for repeated subtraction:

$$24 \div 3 = 8$$

Start at the biggest number (the dividend); subtract groups of divisor.



#### Lower Key Stage 2 (Yr 3/4)

##### Number Line:

Use 'coin card' method  
- find multiples of 1,2,5,10.

$$\begin{array}{l} 1 \times 5 = 5 \\ 2 \times 5 = 10 \\ 5 \times 5 = 25 \\ 10 \times 5 = 50 \end{array}$$

Start at the biggest number (the dividend), subtract groups of divisor.



Short Division:

$$\begin{array}{r} 1 \quad 4 \\ 7 \overline{) 9 \quad 8} \\ \quad 7 \\ \hline \quad 2 \end{array}$$

#### Upper Key Stage 2 (Yr 5/6)

In Year 5 and 6 children should calculate division with remainders. Remainders should be expressed as whole number remainders, decimals and fractions as appropriate to the context.

Short division:

$$\begin{array}{r} 8 \quad 6 \quad r2 \\ 5 \overline{) 4 \quad 3 \quad 2} \\ \quad 4 \quad 0 \\ \hline \quad 3 \quad 2 \end{array}$$

$$\begin{array}{r} 4 \quad 5 \quad r1 \\ 1 \quad 1 \quad 4 \quad 9 \quad 5 \quad 6 \\ \hline \quad \quad \quad \quad \quad \quad 6 \end{array}$$

Answer:  $45\frac{1}{5}$

Long division:

$$\begin{array}{r} 2 \quad 8 \quad 8 \\ 3 \quad 6 \quad 4 \\ 1 \quad 9 \quad 2 \\ 1 \quad 2 \quad 0 \\ \hline 1 \quad 2 \quad 0 \\ 1 \quad 2 \quad 0 \\ \hline 0 \end{array}$$

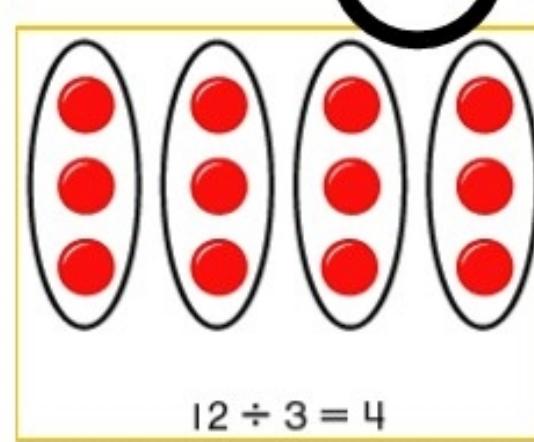
Answer:  $28\frac{8}{3}$

81	82	83	84	85	86	87	88	89	90
81	82	83	84	85	86	87	88	89	90
81	82	83	84	85	86	87	88	89	90
81	82	83	84	85	86	87	88	89	90
81	82	83	84	85	86	87	88	89	90

(Yr 5/6)

digits as well as decimal

ods of addition, the  
be positioned on the  
ill be recorded at the  
l column.



Division is splitting into equal parts or groups. It is the result of "fair sharing".

We use the  $\div$  symbol, or sometimes the / symbol to mean divide

## Vocabulary

÷

Lots of

Groups of

Share

Group

Jumps

Numberline

Equal

Halve

Divide

Division

Divided by

Remainder

Factor

Decimal

Decimal place

Divisible

Multiplication is repeated addition

For example:  $5 \times 3 = 5 + 5 + 5$

It is signified by the symbol X

## Progression in Multiplication Written Calculations

### EYFS

Not appropriate for this year group

Multiplying on a number line

$$4 \times 5 = 20$$



Multiplying on a blank number line

$$7 \times 3 = 21$$



### Lower Key Stage 2 (Yr 3/4)

Use of number line:

$$5 \times 4 = 20$$



Grid method:

×	20	7	
50	1000	350	1350
6	120	42	162

1512

Short multiplication:

$$\begin{array}{r}
 \text{Th H T U} \\
 3\ 4\ 2 \\
 \times \quad 7 \\
 \hline
 14 \\
 280 \\
 2100 \\
 \hline
 2394
 \end{array}$$

$$\begin{array}{r}
 \text{Th H T U} \\
 2\ 1\ 0\ 0 \\
 + 2\ 8\ 0 \\
 \hline
 1\ 4 \\
 + \quad 2\ 3\ 9\ 4 \\
 \hline
 2\ 3\ 9\ 4
 \end{array}$$

Use of various methods should be taught for multiplying numbers with two digits.

Grid:

500
40
9

Short Multiplication:

$$\begin{array}{r}
 2\ 7 \\
 \times \\
 1\ 6\ 4 \\
 \hline
 4\ 2
 \end{array}$$

addition.  
 $+ 5 = 15$   
 $\times 1$   
**Calculations**  
**Key Stage 1 (Yr 1/2)**  
 on a written number line:  
 $20$   
 $5 \quad +5 \quad +5$   
 $10 \quad 15 \quad 20$   
 on a blank number line:  
 $13 \times 3 = 39$   
 $0 \quad 30 \quad 39$

Multiply  
 Multiplication  
 Jumps  
 Multiple  
 Numberline  
 Product  
 Twice  
 Three times  
 Array  
 Row  
 Column  
 Double

### Upper Key Stage 2 (Yr 5/6)

Various methods: grid, short and long multiplication taught where up to 4 digits are being multiplied by with two digits:

$\times$	5
500	3000
40	240
9	54
	3244

multiplication:

1	7	4	1
			6
5	4	4	6
		1	2

Long Multiplication:

$$\begin{array}{r}
 & 1 & 2 \\
 & 1 & 2 & 4 \\
 \times & & 2 & 6 \\
 \hline
 & 7 & 4 & 4 \\
 & 2 & 4 & 8 & 0 \\
 \hline
 & 3 & 2 & 2 & 4 \\
 \hline
 & 1 & 1
 \end{array}$$
